# Package 'cxreg'

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<b>Description</b> Implements 'glmnet'-style complex-valued lasso and complex-valued graphical lasso using a 'pathwise' coordinate descent algorithm for complex-valued parameters. The package provides supporting tools for estimation, simulation, and prediction. See Deb (2024) <doi:10.48550 arxiv.2401.11128=""> for the algorithm description.</doi:10.48550>
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# **Description**

This package fits complex-valued Lasso for regression using coordinate descent. The algorithm is extremely fast, and exploits sparsity in the input x matrix where it exists. A variety of predictions can be made from the fitted models.

#### **Details**

This package also provides fitting for complex-valued graphical Lasso using coordinate descent. The function is built upon classo with covariate updates, just as the regular real-valued coordinate descent algorithm for graphical Lasso.

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Very simple to use. Accepts x,y data for penalized regression models, and produces the regularization paths over a grid of values for the tuning parameters lambda. Similarly, accepts S,n data for penalized Gaussian likelihood, and produce the regularization paths over a grid of values for the tuning parameter lambda.

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#### References

Deb, N., Kuceyeski, A., Basu, S. (2024) Regularized Estimation of Sparse Spectral Precision Matrices, https://arxiv.org/abs/2401.11128.

# **Examples**

```
set.seed(1234)
x \leftarrow array(rnorm(100*20), c(100,20)) + (1+1i) * array(rnorm(100*20), c(100,20))
for (j in 1:20) x[,j] \leftarrow x[,j] / sqrt(mean(Mod(x[,j])^2))
e <- rnorm(100) + (1+1i) * rnorm(100)
b \leftarrow c(1, -1, rep(0, 18)) + (1+1i) * c(-0.5, 2, rep(0, 18))
y <- x %*% b + e
fit <- classo(x, y)</pre>
predict(fit, newx = x[1:5, ], s = c(0.01, 0.005))
predict(fit, type = "coef")
plot(fit, xvar = "lambda")
p < -30
n <- 500
C <- diag(0.7, p)
C[row(C) == col(C) + 1] <- 0.3
C[row(C) == col(C) - 1] <- 0.3
Sigma <- solve(C)</pre>
set.seed(1010)
m <- floor(sqrt(n)); j <- 1</pre>
X_t \leftarrow mvtnorm::rmvnorm(n = n, mean = rep(0, p), sigma = Sigma)
d_j \leftarrow dft.X(X_t,j,m)
f_j_hat <- t(d_j) %*% Conj(d_j) / (2*m+1)
fit <- cglasso(S=f_j_hat, nobs=n,type="I")</pre>
plot(fit$Theta_list,index=fit$min_index,type="mod",label=FALSE)
```

buildPredmat

**Build Prediction Matrix** 

#### **Description**

These are not intended for use by users. Constructs a prediction matrix for cross-validation folds, using the coefficient paths in outlist. Inspired by internal functions in the glmnet package.

#### Usage

```
buildPredmat(outlist, lambda, x, foldid, alignment, ...)
```

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#### **Arguments**

outlist A list of fitted models.

lambda A vector of penalty values.

x A predictor matrix.

foldid Fold identifiers.

alignment Alignment method (not used).

... Other arguments

#### Value

The return value depends on the method; for the default method, see buildPredmat.default.

# **Description**

These are not intended for use by users. Constructs a prediction matrix for cross-validation folds, using the coefficient paths in outlist. Inspired by internal functions in the **glmnet** package.

# Usage

```
## Default S3 method:
buildPredmat(outlist, lambda, x, foldid, alignment, ...)
```

#### **Arguments**

outlist A list of fitted models.

lambda A vector of penalty values.

x A predictor matrix.

foldid Fold identifiers.

alignment Alignment method (not used).

... Other arguments

# Value

A numeric matrix of predicted values with dimensions nrow(x) by length(lambda). Rows correspond to observations and columns correspond to penalty values.

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cglasso

fit a complex-valued graphical lasso

#### **Description**

Fit a complex-valued graphical lasso for spectral precision matrix (inverse spectral density matrix) via a complex variable-wise coordinate descent algorithm for classo with covariates update.

# Usage

```
cglasso(
   S,
   D = NULL,
   type = c("I", "II"),
   nobs,
   lambda = NULL,
   nlambda = 50,
   lambda.min.ratio = ifelse(nobs < p, 0.01, 1e-04),
   W.init = NULL,
   stopping_rule = TRUE,
   stop_criterion = c("EBIC", "AIC", "RMSE"),
   maxit = 500,
   thresh = 1e-04,
   trace.it = 0,
   ...
)</pre>
```

#### **Arguments**

S

p x p-dimensional symmetric spectral density (or spectral coherence) matrix. S is considered as being computed by average smoothed periodogram (the bandwidth is computed by using the given nobs).

D

The p x p-dimensional diagonal matrix with spectral densities as the diagonal entries. Default is NULL. If D is not provided, diagonals of S are chosen.

type

A logical flag to choose the formulation to solve. Default is I. If type is I, the algorithm solves CGLASSO-I in the reference,

$$D^{-1/2}\left(\arg\min_{\Theta}\operatorname{Tr}\left[\hat{R}\hat{\Theta}\right] - \log\det\Theta + \sum_{i\neq j}|\Theta_{ij}|\right)D^{-1/2}$$

for the given D. If type is II, the algorithm solves CGLASSO-II in the reference. It is for each iterative classo with covariate update, the squared-root of scale matrix  $D^{-1/2}$  is multiplied. Please refer to the equation (5.2) in the reference for the details.

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nobs Number of observations used in computation of the spectral density matrix S.

This quantity is need to compute the Fourier frequency, extended BIC, and band-

width for the average smoothed periodogram.

lambda A user supplied lambda sequence. Typical usage is to have the program compute

its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a

single value for lambda

nlambda The number of lambda values - default is 50.

lambda.min.ratio

Smallest value for lambda, as a fraction of lambda.max, the (data derived) entry value (i.e. the smallest value for which all coefficients are zero). The default depends on the sample size nobs relative to the number of variables nvars. If nobs > p, the default is 0.0001, close to zero. If nobs < p, the default is 0.01.

W. init Logical flag whether the initially estimated spectral density matrix is given. De-

fault is NULL.

stopping\_rule Logical flag if the algorithm is terminated by stopping rule. If the algorithm is

early terminated ,not all estimates for initially designated lambdas are explored.

stop\_criterion Stopping criterion for early termination. Default is EBIC (Extended BIC). Alter-

natively, AIC (AIC) and RMSE (root mean squared error between two consecutive

estimates) can be used.

maxit Maximum number of iterations of both outer and inner loops. Default 500.

thresh Convergence threshold for coordinate descent. Default is 1e-4.

trace.it If trace.it=1, then a progress bar is displayed;

... Other arguments that can be passed to cglasso useful for big models that take

a long time to fit.

#### **Details**

The sequence of models implied by lambda is fit by coordinate descent.

# Value

An object with class "cglassofit" and "cglasso".

stop\_arr Sequence of values of information criterion for a fixed lambda.

stop\_criterion Stopping criterion used.

min\_index The index for lambda that minimizes the value of the information criterion.

lambda\_grid Sequence of lambdas used.

Theta\_list Estimated inverse spectral matrix for each fixed lambda. It is provided in the

list.

type Type of the formulation used, either CGALSSO-I or CGLASSO-II.

scale Whether the spectral density matrix (covariance) or spectral coherence (coher-

ence) is given.

D Used scale diagonal matrix.

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#### Author(s)

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#### References

Deb, N., Kuceyeski, A., Basu, S. (2024) Regularized Estimation of Sparse Spectral Precision Matrices, https://arxiv.org/abs/2401.11128.

# **Examples**

```
p <- 30
n <- 500
C <- diag(0.7, p)
C[row(C) == col(C) + 1] <- 0.3
C[row(C) == col(C) - 1] <- 0.3
Sigma <- solve(C)
set.seed(1010)
m <- floor(sqrt(n)); j <- 1
X_t <- mvtnorm::rmvnorm(n = n, mean = rep(0, p), sigma = Sigma)
d_j <- dft.X(X_t,j,m)
f_j_hat <- t(d_j) %*% Conj(d_j) / (2*m+1)
fit <- cglasso(S=f_j_hat, nobs=n)</pre>
```

cglasso.path

fit a complex-valued graphical Lasso for a path of lambda values

#### **Description**

Fit a complex-valued graphical Lasso formulation for a path of lambda values. cglasso.path solves the penalized Gaussian maximum likelihood problem for a path of lambda values.

# Usage

```
cglasso.path(
   S,
   D,
   type,
   nobs,
   lambda,
   nlambda,
   lambda.min.ratio,
   W.init,
   stopping_rule,
   stop_criterion,
   maxit = maxit,
   thresh = thresh,
   trace.it = trace.it,
```

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)

#### **Arguments**

D

S p x p-dimensional symmetric spectral density (or spectral coherence) matrix. S is considered as being computed by average smoothed periodogram (the bandwidth is computed by using the given nobs).

The p x p-dimensional diagonal matrix with spectral densities as the diagonal entries. Default is NULL. If D is not provided, diagonals of S are chosen.

type Logical flag to choose the formulation to solve. Default is I. If type is I, the algorithm solves CGLASSO-I in the reference,

$$D^{-1/2}(\arg\min_{\Theta} Tr[\hat{R}\hat{\Theta}] - \log\det\Theta + \sum_{i \neq j} |\Theta_{ij}|)D^{-1/2}$$

for the given \$D\$. If type is II, the algorithm solves CGLASSO-II in the reference. It is for each iterative classo with covariate update, the scale matrix D is multiplied. Please see the reference for the details of the iterative updates.

Number of observations used in computation of the spectral density matrix S. This quantity is need to compute the Fourier frequency, extended BIC, and bandwidth for the average smoothed periodogram.

A user supplied lambda sequence. Typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda

nlambda The number of lambda values - default is 50. lambda.min.ratio

> Smallest value for lambda, as a fraction of lambda. max, the (data derived) entry value (i.e. the smallest value for which all coefficients are zero). The default depends on the sample size nobs relative to the number of variables nvar. If nobs > p, the default is 0.0001, close to zero. If nobs < p, the default is 0.01.

Logical flag whether the initially estimated spectral density matrix is given. Default is NULL.

> Logical flag if the algorithm is terminated by stopping rule. If the algorithm is early terminated, not all estimates for initially designated lambdas are explored.

> Stopping criterion for early termination. Default is EBIC (Extended BIC). Alternatively, AIC (AIC) and RMSE (root mean squared error between two consecutive estimates) can be used.

Maximum number of iterations of both outer and inner loops. Default 500.

thresh Convergence threshold for coordinate descent. Default is 1e-4.

If trace.it=1, then a progress bar is displayed; useful for big models that take trace.it a long time to fit.

Other arguments that can be passed to cglasso

nobs

lambda

W.init

stop\_criterion

stopping\_rule

maxit

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#### Value

An object with class "cglassofit" and "cglasso".

a0 Intercept sequence of length length(lambda).

beta A nvar x length(lambda) matrix of coefficients, stored in sparse matrix for-

mat.

df The number of nonzero coefficients for each value of lambda.

dim Dimension of coefficient matrix.

lambda The actual sequence of lambda values used. When alpha=0, the largest lambda

reported does not quite give the zero coefficients reported (lambda=inf would in principle). Instead, the largest lambda for alpha=0.001 is used, and the sequence

of lambda values is derived from this.

dev The fraction of (null) deviance explained. The deviance calculations incorporate

weights if present in the model. The deviance is defined to be 2\*(loglike\_sat - loglike), where loglike\_sat is the log-likelihood for the saturated model (a model

with a free parameter per observation). Hence dev=1-dev/nulldev.

nulldev Null deviance (per observation). This is defined to be 2\*(loglike\_sat -loglike(Null)).

The null model refers to the intercept model.

npasses Total passes over the data summed over all lambda values.

jerr Error flag, for warnings and errors (largely for internal debugging).

call The call that produced this object.

family Family used for the model.

Number of observations.

#' @return An object with class "cglassofit" and "cglasso".

stop\_arr Sequence of values of information criterion for a fixed lambda.

stop\_criterion Stopping criterion used.

min\_index The index for lambda that minimizes the value of the information criterion.

lambda\_grid Sequence of lambdas used.

Theta\_hat Estimated inverse spectral matrix for each fixed lambda. It is provided in the

list.

type Type of the formulation used, either CGALSSO-I or CGLASSO-II.

scale Whether the spectral density matrix (covariance) or spectral coherence (coher-

ence) is given.

D Used scale diagonal matrix.

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cglasso\_example

Example Data for CGLASSO

# **Description**

A synthetic dataset used to illustrate complex-valued graphical Lasso.

# Usage

```
data(cglasso_example)
```

#### **Format**

A list with components:

- S Spectral density matrix
- n Sample size

classo

fit a complex-valued lasso

# **Description**

Fit a complex-valued lasso formulation via complex update coordinate descent algorithm. By defining a field isomorphism between complex values and its 2 by 2 representation, it enables to update each coordinate of the solution as a regular coordinate descent algorithm.

# Usage

```
classo(
   x,
   y,
   weights = NULL,
   lambda = NULL,
   nlambda = 100,
   lambda.min.ratio = ifelse(nobs < nvars, 0.01, 1e-04),
   standardize = TRUE,
   intercept = FALSE,
   maxit = 10000,
   thresh = 1e-07,
   trace.it = 0,
   ...
)</pre>
```

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#### **Arguments**

x input matrix, of dimension nobs x nvars; each row is an observation vector.

Requirement: nvars >1; in other words, x should have 2 or more columns.

y response variable.

weights observation weights. Default is 1 for each observation.

lambda A user supplied lambda sequence. Typical usage is to have the program compute

its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda (for predictions after CV use predict() instead). Supply instead a decreasing sequence of lambda values. classo relies on its warms starts for speed, and its often faster to fit a whole path than compute a

single fit.

nlambda The number of lambda values - default is 100.

lambda.min.ratio

Smallest value for lambda, as a fraction of lambda.max, the (data derived) entry value (i.e. the smallest value for which all coefficients are zero). The default depends on the sample size nobs relative to the number of variables nvars. If nobs > nvars, the default is 0.0001, close to zero. If nobs < nvars, the default is 0.01. A very small value of lambda.min.ratio will lead to a saturated fit in

the nobs < nvars case.

standardize Logical flag for x variable standardization, prior to fitting the model sequence.

The coefficients are always returned on the original scale. Default is standardize=TRUE.

intercept Should intercept(s) set to zero (default=FALSE) or be fitted (TRUE).

maxit Maximum number of iterations of outer loop. Default 10,000.

thresh Convergence threshold for coordinate descent. Each inner coordinate-descent

loop continues until the maximum change in the objective after any coefficient

update is less than thresh times the null deviance. Defaults value is 1e-7.

trace.it If trace.it=1, then a progress bar is displayed; useful for big models that take

a long time to fit.

... Other arguments that can be passed to classo

#### **Details**

The sequence of models implied by lambda is fit by coordinate descent.

#### Value

An object with class "classofit" and "classo".

a0 Intercept sequence of length length(lambda).

beta A nvars x length(lambda) matrix of coefficients, stored in sparse matrix for-

mat.

df The number of nonzero coefficients for each value of lambda.

dim Dimension of coefficient matrix.

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lambda	The actual sequence of lambda values used. When alpha=0, the largest lambda reported does not quite give the zero coefficients reported (lambda=inf would in principle). Instead, the largest lambda for alpha=0.001 is used, and the sequence of lambda values is derived from this.
dev	The fraction of (null) deviance explained. The deviance calculations incorporate weights if present in the model. The deviance is defined to be 2*(loglike_sat - loglike), where loglike_sat is the log-likelihood for the saturated model (a model with a free parameter per observation). Hence dev=1-dev/nulldev.
nulldev	Null deviance (per observation). This is defined to be $2*(loglike\_sat - loglike(Null))$ . The null model refers to the intercept model.
npasses	Total passes over the data summed over all lambda values.
jerr	Error flag, for warnings and errors (largely for internal debugging).
call	The call that produced this object.
family	Family used for the model.
nobs	Number of observations.

# Author(s)

Navonil Deb, Younghoon Kim, Sumanta Basu Maintainer: Younghoon Kim <yk748@cornell.edu>

#### References

Deb, N., Kuceyeski, A., Basu, S. (2024) Regularized Estimation of Sparse Spectral Precision Matrices, https://arxiv.org/abs/2401.11128.

# **Examples**

```
set.seed(1010)
n = 1000
p = 200
x = array(rnorm(n*p), c(n,p)) + (1+1i) * array(rnorm(n*p), c(n,p))
for (j in 1:p) x[,j] = x[,j] / sqrt(mean(Mod(x[,j])^2))
e = rnorm(n) + (1+1i) * rnorm(n)
b = c(1, -1, rep(0, p-2)) + (1+1i) * c(-0.5, 2, rep(0, p-2))
y = x **% b + e
fit.test = classo(x, y)
```

classo.control

internal classo parameters

# **Description**

View and/or change the factory default parameters in classo

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# Usage

```
classo.control(
  fdev = 1e-05,
  devmax = 0.999,
  eps = 1e-06,
  big = 9.9e+35,
  mnlam = 5,
  pmin = 1e-09,
  exmx = 250,
  prec = 1e-10,
  mxit = 100,
  itrace = 0,
  epsnr = 1e-06,
  mxitnr = 25,
  factory = TRUE
)
```

# Arguments

fdev	minimum fractional change in deviance for stopping path; factory default = 1.0e-5
devmax	maximum fraction of explained deviance for stopping path; factory default = $0.999$
eps	minimum value of lambda.min.ratio (see classo); factory default= 1.0e-6
big	large floating point number; factory default = 9.9e35. Inf in definition of upper.limit is set to big
mnlam	minimum number of path points (lambda values) allowed; factory default = 5
pmin	minimum probability for any class. factory default = $1.0e-9$ . Note that this implies a pmax of $1$ -pmin.
exmx	maximum allowed exponent. factory default = 250.0
prec	convergence threshold for multi response bounds adjustment solution. factory default = $1.0e-10$
mxit	maximum iterations for multiresponse bounds adjustment solution. factory default = $100$
itrace	If 1 then progress bar is displayed when running classo and cv.classo. factory default = $0$
epsnr	convergence threshold for classo.fit. factory default = 1.0e-6
mxitnr	maximum iterations for the IRLS loop in classo.fit. factory default = 25
factory	If TRUE, reset all the parameters to the factory default; default is FALSE

# **Details**

If called with no arguments, classo.control() returns a list with the current settings of these parameters. Any arguments included in the call sets those parameters to the new values, and then silently returns. The values set are persistent for the duration of the R session.

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#### Value

A list with named elements as in the argument list

#### See Also

classo

#### **Examples**

```
classo.control(fdev = 0) #continue along path even though not much changes classo.control() # view current settings classo.control(factory = TRUE) # reset all the parameters to their default
```

classo.path

fit a complex-valued lasso for a path of lambda values

# **Description**

Fit a complex-valued lasso formulation for a path of lambda values. classo.path solves the Lasso problem for a path of lambda values.

#### Usage

```
classo.path(
    x,
    y,
    weights = NULL,
    standardize = FALSE,
    lambda = NULL,
    nlambda = 100,
    lambda.min.ratio = ifelse(nobs < nvars, 0.01, 1e-04),
    intercept = FALSE,
    thresh = 1e-10,
    maxit = 1e+05,
    trace.it = 0,
    ...
)</pre>
```

#### **Arguments**

x Complex-valued input matrix, of dimension nobs by nvar; each row is an observation vector.

y Complex-valued response variable, nobs dimensional vector.

weights Observation weights. Default is 1 for each observation.

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standardize Logical flag for x variable standardize beforehand; i.e. for n and p by nobs and

nvar,

 $||X_i|| = \sqrt{n}$  for all  $j = 1, \ldots, p$ 

is satisfied for the input x. Default is FALSE.

lambda A user supplied lambda sequence. Default is NULL.

nlambda The number of lambda values. Default is 100.

lambda.min.ratio

If nobs < nvars, the default is 0.01.

intercept Should intercept be set to zero (default=FALSE) or fitted (FALSE)? This default

is reversed from glmnet package.

thresh Convergence threshold for coordinate descent. Each inner coordinate-descent

loop continues until the maximum change in the objective after any coefficient update is less than thresh times the null deviance. Default value is 1e-10.

maxit Maximum number of iterations of outer loop. Default 10,000.

trace.it Controls how much information is printed to screen. Default is trace.it=0 (no

information printed). If trace.it=1, a progress bar is displayed. If trace.it=2, some information about the fitting procedure is printed to the console as the

model is being fitted.

... Other arguments that can be passed to classo

#### Value

An object with class "classofit" and "classo".

a0 Intercept sequence of length length(lambda).

beta A nvars x length(lambda) matrix of coefficients, stored in sparse matrix for-

mat.

df The number of nonzero coefficients for each value of lambda.

dim Dimension of coefficient matrix.

lambda The actual sequence of lambda values used. When alpha=0, the largest lambda

reported does not quite give the zero coefficients reported (lambda=inf would in principle). Instead, the largest lambda for alpha=0.001 is used, and the sequence

of lambda values is derived from this.

dev.ratio The fraction of (null) deviance explained. The deviance calculations incorporate

weights if present in the model. The deviance is defined to be  $2*(loglike\_sat - loglike)$ , where loglike\\_sat is the log-likelihood for the saturated model (a model

with a free parameter per observation). Hence dev.ratio=1-dev/nulldev.

nulldev Null deviance (per observation). This is defined to be 2\*(loglike\_sat -loglike(Null)).

The null model refers to the intercept model.

npasses Total passes over the data summed over all lambda values.

jerr Error flag, for warnings and errors (largely for internal debugging).

call The call that produced this object.

family Family used for the model. nobs Number of observations.

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classo\_example

Example Data for CLASSO

# **Description**

A toy example demonstrating complex-valued lasso.

# Usage

```
data(classo_example)
```

# **Format**

A list with components:

- X Design matrix
- Y Response vector

coef.classo

Extract coefficients from a classo object

# Description

Similar to other predict methods, this functions predicts fitted values, coefficients and more from a fitted "classo" object.

# Usage

```
## S3 method for class 'classo'
coef(object, s = NULL, exact = FALSE, ...)

## S3 method for class 'classo'
predict(
   object,
   newx,
   s = NULL,
   type = c("response", "coefficients", "nonzero"),
   exact = FALSE,
   ...
)
```

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#### **Arguments**

object Fitted "classo" model object.

Value(s) of the penalty parameter lambda at which predictions are required. De-

fault is the entire sequence used to create the model.

exact This argument is relevant only when predictions are made at values of s (lambda)

different from those used in the fitting of the original model. If exact=FALSE (default), then the predict function uses linear interpolation to make predictions for values of s (lambda) that do not coincide with those used in the fitting algorithm. While this is often a good approximation, it can sometimes be a bit coarse. With exact=TRUE, these different values of s are merged (and sorted) with object\$lambda, and the model is refit before predictions are made. In this case, it is required to supply the original data x= and y= as additional named arguments to predict() or coef(). The workhorse predict.classo() needs to update the model, and so needs the data used to create it. The same is true of weights if these were used in the original call. Failure to do so will result in an

error. type="nonzero")

... This is the mechanism for passing arguments like x= when exact=TRUE; seeexact

argument.

newx Matrix of new values for x at which predictions are to be made. Must be a

matrix. This #' argument is not used for type=c("coefficients", "nonzero")

type Type of prediction required. Type "link" givee the fitted values for "gaussian".

Type "response" is equivalent to type "link". Type "coefficients" computes the coefficients at the requested values for s. Type "nonzero" returns a

list of the indices of the nonzero coefficients for each value of s.

#### **Details**

This function actually calls NextMethod(). coef(...) is equivalent to predict(type="coefficients",...)

#### Value

The object returned depends on type.

#### Author(s)

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#### References

Deb, N., Kuceyeski, A. and Basu, S. (2024) Regularized estimation of sparse spectral precision matrices (2024), Preprint, https://arxiv.org/abs/2401.11128.

#### See Also

classo, and print, and coef methods, and cv.classo.

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cv.classo

Cross-validation for classo

# Description

Does k-fold cross-validation for classo, produces a plot, and returns a value for lambda

#### Usage

```
cv.classo(
    x,
    y,
    weights = NULL,
    lambda = NULL,
    nfolds = 10,
    foldid = NULL,
    alignment = c("lambda", "fraction"),
    keep = FALSE,
    parallel = FALSE,
    trace.it = 0,
    ...
)
```

#### **Arguments**

x x matrix as in classo.y response y as in classo.

weights Observation weights; defaults to 1 per observation

Optional user-supplied lambda sequence; default is NULL, and classo chooses its own sequence. Note that this is done for the full model (master sequence),

and separately for each fold. The fits are then aligned using the master sequence (see the alignment argument for additional details). Adapting lambda for each fold leads to better convergence. When lambda is supplied, the same sequence

is used everywhere.

nfolds number of folds - default is 10. Although nfolds can be as large as the sample

size (leave-one-out CV), it is not recommended for large dataset. Smallest value

allowable is nfolds=3

foldid an optional vector of values between 1 and nfolds identifying what fold each

observation is in. If supplied, nfolds can be missing.

alignment This is an experimental argument, designed to fix the problems users were hav-

ing with CV, with possible values "lambda" (the default) else "fraction". With "lambda" the lambda values from the master fit (on all the data) are used to line up the predictions from each of the folds. In some cases this can give strange values, since the effective lambda values in each fold could be quite different.

cv.classo 19

With "fraction" we line up the predictions in each fold according to the fraction of progress along the regularization. If in the call a lambda argument is also

provided, alignment="fraction" is ignored (with a warning).

keep If keep=TRUE, a prevalidated array is returned containing fitted values for each

observation and each value of lambda. This means these fits are computed with this observation and the rest of its fold omitted. The foldid vector is also re-

turned. Default is keep=FALSE.

parallel If TRUE, use parallel for each to fit each fold. Must register parallel before hand,

such as doMC or others. Currently it is unavailable.

trace.it If trace.it=1, then progress bars are displayed; useful for big models that take

a long time to fit. Limited tracing if parallel=TRUE

... Other arguments that can be passed to classo

#### **Details**

The function runs classo nfolds+1 times; the first to get the lambda sequence, and then the remainder to compute the fit with each of the folds omitted. The error is accumulated, and the average error and standard deviation over the folds is computed.

Note that the results of cv.classo are random, since the folds are selected at random. Users can reduce this randomness by running cv.classo many times, and averaging the error curves.

#### Value

an object of class "cv.classo" is returned, which is a list with the ingredients of the cross-validation fit.

lambda the values of lambda used in the fits.

cvm The mean cross-validated error - a vector of length length(lambda).

cvsd estimate of standard error of cvm.

cvup upper curve = cvm+cvsd.
cvlo lower curve = cvm-cvsd.

nzero number of non-zero coefficients at each lambda.

name a text string indicating type of measure for plotting purposes).

classo.fit a fitted classo object for the full data.

lambda.min value of lambda that gives minimum cvm.

lambda.1se largest value of lambda such that error is within 1 standard error of the mini-

mum.

fit.preval if keep=TRUE, this is the array of pre-validated fits. Some entries can be NA, if

that and subsequent values of lambda are not reached for that fold

foldid if keep=TRUE, the fold assignments used

index a one column matrix with the indices of lambda.min and lambda.1se in the

sequence of coefficients, fits etc.

20 cxreg

#### Author(s)

```
Navonil Deb, Younghoon Kim, Sumanta Basu
Maintainer: Younghoon Kim <yk748@cornell.edu>
```

#### See Also

classo and plot and coef methods for "cv.classo".

#### **Examples**

```
set.seed(1010)
n = 1000
p = 200
x = array(rnorm(n*p), c(n,p)) + (1+1i) * array(rnorm(n*p), c(n,p))
for (j in 1:p) x[,j] = x[,j] / sqrt(mean(Mod(x[,j])^2))
e = rnorm(n) + (1+1i) * rnorm(n)
b = c(1, -1, rep(0, p-2)) + (1+1i) * c(-0.5, 2, rep(0, p-2))
y = x %*% b + e
cv.test = cv.classo(x,y)
```

cxreg

Simulated data for the cxreg vignette

# Description

Simple simulated data, used to demonstrate the features of cxreg

#### **Format**

Data objects used to demonstrate features in the cxreg vignette

#### **Details**

These datasets are artificial, and are used to test out some of the features of exreg.

#### **Examples**

```
data(classo_example)
x <- classo_example$x
y <- classo_example$y
classo(x,y)

data(cglasso_example)
f_hat <- cglasso_example$f_hat
n <- cglasso_example$n
cglasso(S=f_hat,type="I",nobs=n)
cglasso(S=f_hat,type="II",nobs=n)</pre>
```

dft.X 21

dft.X

Discrete Fourier Transform of matrix X

# **Description**

Computes the (normalized) discrete Fourier transform (DFT) of a matrix X row-wise using mvfft, and extracts a window of frequencies centered at a target index.

# Usage

```
dft.X(X, j, m)
```

# **Arguments**

X	A numeric matrix of size $nobs \times nvar$ , where DFT is applied across the rows (time points).
j	An integer index in $1, \ldots, nobs$ around which the frequency window is centered.
m	A non-negative integer specifying the window half-width. The function returns 2m + 1 DFT components centered around j.

#### Value

A complex-valued matrix of dimension  $(2m + 1) \times nvar$  representing selected DFT components of the original matrix.

fixm	Fixes indices that fall outside the valid range 1:n using circular (mod-
	ulo) wrapping.

# Description

Fixes indices that fall outside the valid range 1:n using circular (modulo) wrapping.

# Usage

```
fixm(v, n)
```

# **Arguments**

v An integer vector of indices.

n A positive integer giving the length of the domain; valid indices are 1 to nobs.

#### Value

An integer vector of the same length as v, with all values wrapped into the range 1 to n.

22 plot.cglasso

plot.cglasso

plot heatmap from a "cglasso" object

# Description

Produces plot of the estimated inverse spectral matrix for a fitted "cglasso" object. A inverse spectral matrix profile plot is produced.

# Usage

```
## S3 method for class 'cglasso'
plot(
    x,
    index,
    type = c("real", "imaginary", "mod", "both"),
    label = FALSE,
    ...
)
```

# Arguments

X	fitted "cglasso" model
index	For which inverse spectral matrix profile is the plot to be drawn? Default is 1. The index must be provided within the length of the sequence of lambdas.
type	Whether the plot is for real or imaginary part, or both, or in modulus (mod; absolute scale). Default is mod.
label	If TRUE, label the axes with variable names.
	Other graphical parameters to plot.

# Value

No return value, called for side effects (produces a plot).

# Author(s)

```
Navonil Deb, Younghoon Kim, Sumanta Basu
Maintainer: Younghoon Kim <yk748@cornell.edu>
```

# See Also

cglasso

plot.classo 23

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plot coefficients from a "classo" object

# Description

Produces a coefficient profile plot of the coefficient paths for a fitted "classo" object.

# Usage

```
## S3 method for class 'classo'
plot(x, xvar = c("norm", "lambda", "dev"), label = FALSE, ...)
```

# Arguments

X	fitted "classo" model
xvar	What is on the X-axis. "norm" plots against the L1-norm of the coefficients, "lambda" against the log-lambda sequence, and "dev" against the percent deviance explained.
label	If TRUE, label the curves with variable sequence numbers.
• • •	Other graphical parameters to plot

# **Details**

A coefficient profile plot is produced.

# Value

No return value, called for side effects (produces a plot).

# Author(s)

```
Navonil Deb, Younghoon Kim, Sumanta Basu
Maintainer: Younghoon Kim <yk748@cornell.edu>
```

#### See Also

classo

24 plot.cv.classo

plot.cv.classo

plot the cross-validation curve produced by cv.classo

#### **Description**

Plots the cross-validation curve, and upper and lower standard deviation curves, as a function of the lambda values used.

#### Usage

```
## S3 method for class 'cv.classo'
plot(x, sign.lambda = 1, ...)
```

#### **Arguments**

```
x fitted "cv.classo" object
sign.lambda Either plot against log(lambda) (default) or its negative if sign.lambda=-1.
Other graphical parameters to plot.
```

#### **Details**

A plot is produced, and nothing is returned.

#### Value

No return value, called for side effects (produces a plot).

### Author(s)

```
Navonil Deb, Younghoon Kim, Sumanta Basu
Maintainer: Younghoon Kim <yk748@cornell.edu>
```

#### See Also

classo and plot methods for "cv.classo".

# **Examples**

```
set.seed(1010)
n = 1000
p = 200
x = array(rnorm(n*p), c(n,p)) + (1+1i) * array(rnorm(n*p), c(n,p))
for (j in 1:p) x[,j] = x[,j] / sqrt(mean(Mod(x[,j])^2))
e = rnorm(n) + (1+1i) * rnorm(n)
b = c(1, -1, rep(0, p-2)) + (1+1i) * c(-0.5, 2, rep(0, p-2))
y = x %*% b + e
cv.test = cv.classo(x,y)
plot(cv.test)
```

predict.cv.classo 25

predict.cv.classo	make predictions from a "cv.classo" object.	
	I	

# Description

This function makes predictions from a cross-validated classo model, using the stored "classo.fit" object.

# Usage

```
## S3 method for class 'cv.classo'
predict(object, newx, s = c("lambda.1se", "lambda.min"), ...)
```

# Arguments

object	Fitted "cv.classo" object.
newx	Matrix of new values for x at which predictions are to be made. Must be a matrix
S	Value(s) of the penalty parameter lambda at which predictions are required. Default is the value s="lambda.1se" stored on the CV object. Alternatively s="lambda.min" can be used. If s is numeric, it is taken as the value(s) of lambda to be used. (For historical reasons we use the symbol 's' rather than 'lambda' to reference this parameter)
	Not used. Other arguments to predict.

#### **Details**

This function makes it easier to use the results of cross-validation to make a prediction.

# Value

The object returned depends on the ... argument which is passed on to the predict method for classo objects.

# Author(s)

```
Younghoon Kim, Navonil Deb, Sumanta Basu
Maintainer: Younghoon Kim yk748@cornell.edu
```

#### See Also

classo, and print, and coef methods, and cv.classo.

26 print.cv.classo

print.classo

print a classo object

# Description

Print a summary of the classo path at each step along the path.

#### Usage

```
## S3 method for class 'classo'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

### **Arguments**

x fitted classo objectdigits significant digits in printout

... additional print arguments

# **Details**

The call that produced the object x is printed, followed by a three-column matrix with columns Df, %Dev and Lambda. The Df column is the number of nonzero coefficients (Df is a reasonable name only for lasso fits). %Dev is the percent deviance explained (relative to the null deviance).

#### Value

The matrix above is silently returned

#### See Also

classo, predict and coef methods.

print.cv.classo

print a cross-validated classo object

# **Description**

Print a summary of the results of cross-validation for a classo model.

## Usage

```
## S3 method for class 'cv.classo'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

print.cv.classo 27

# **Arguments**

x fitted 'cv.classo' objectdigits significant digits in printoutadditional print arguments

#### **Details**

A summary of the cross-validated fit is produced, slightly different for a 'cv.relaxed' object than for a 'cv.classo' object. Note that a 'cv.relaxed' object inherits from class 'cv.classo', so by directly invoking print.cv.classo(object) will print the summary as if relax=TRUE had not been used.

# Value

The matrix above is silently returned

# See Also

classo, predict and coef methods.

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