Package 'TSLA'

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Description

This package provides functions and visualization tools for fitting the Tree-Guided Rare Feature Selection and Logic Aggregation model.

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cal2norm	Calculate group norms	

Description

Function to output group norms on the gamma coefficients based on g_idx and C2 matrix.

Usage

```
cal2norm(u, g_idx, type)
```

Arguments

u	C2*gamma.coef, gamma.coef is the estimated node coefficient vector, C2 matrix is the output from function get_tree_object(), which gives the weights of the
	groups.
g_idx	Group structure matrix defined by the C2 matrix. See details in get_tree_object().
type	If type == 1, return sum of group norms; else return individual norm for each
	group.

Value

Sum of group norms or individual group norms.

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ClassificationExample Synthesic for the classification example

Description

Synthetic data used to illustrate how to use TSLA with classification.

Usage

```
data(ClassificationExample)
```

Format

List containing the following elements:

tree.org Original tree structure with 42 leaf nodes and 5 different levels.

x.org Original design matrix with 42 binary features and 400 observations.

- x1 Unpenalized covariate.
- y Continuous response of length 400.

coef_TSLA

Get coefficients from a fitted TSLA model

Description

Get coefficients from a TSLA.fit object.

Usage

```
coef_TSLA(object, ...)
```

Arguments

object A fit output from TSLA.fit().
... Other parameters.

Value

A list of coefficients for each combination of λ and α . The first dimension is indexed by the coefficient, the second dimension is indexed by λ , and the third dimension is indexed by α .

Intercept Intercept.

cov.coef Coefficients for unpenalized features.

gamma.coef Node coefficients. Also see details in getetmat().

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beta.coef	Regression coefficients. Each coefficient is multiplied by $(-1)^{r-1}$, where r is the order of the corresponding interaction term. Also see details in getetmat().
beta.coef.adj	Regression coefficients β . This is the common regression coefficient vector. It corresponds to x.expand.adj and A.adj.

cv.TSLA

Cross validation for TSLA

Description

Conduct cross validation to select the optimal tuning parameters in TSLA.

Usage

```
cv.TSLA(
   y,
   X_1 = NULL,
   X_2,
   treemat,
   family = c("ls", "logit"),
   penalty = c("CL2", "RFS-Sum"),
   pred.loss = c("MSE", "AUC", "deviance"),
   gamma.init = NULL,
   weight = NULL,
   nfolds = 5,
   group.weight = NULL,
   feature.weight = NULL,
   control = list(),
   modstr = list()
)
```

Arguments

у	Response in matrix form, continuous for family = "ls" and binary (0/1) for family = "logit".
X_1	Design matrix for unpenalized features (excluding intercept). Need to be in the matrix form.
X_2	Expanded design matrix for penalty = "CL2"; Original design matrix for penalty = "RFS-Sum". Need to be in the matrix form.
treemat	Expanded tree structure in matrix form for penalty = "CL2"; Original structure for penalty = "RFS-Sum".
family	Two options. Use "ls" for least square problems and "logit" for logistic regression problems.
penalty	Two options for group penalty on γ , "CL2" or "RFS-Sum".

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pred.loss Model performance metrics. If family="ls", default is "MSE" (mean squared

error). If family="logit", default is "AUC". For logistic model, another option

is "deviance".

gamma.init Initial value for the optimization. Default is a zero vector. The length should

equal to 1+ncol(X_1)+ncol(A). See details of A in get_tree_obj().

weight A vector of length two and it is used for logistic regression only. The first

element corresponds to weight of y=1 and the second element corresponds to

weight of y=0.

nfolds Number of cross validation folds. Default is 5.

group.weight User-defined weights for group penalty. Need to be a vector and the length

equals to the number of groups.

feature.weight User-defined weights for each predictor after expansion.

control A list of parameters controlling algorithm convergence. Default values: tol =

1e-5, convergence tolerance; maxit = 10000, maximum number of iterations;

mu = 1e-3, smoothness parameter in SPG.

modstr A list of parameters controlling tuning parameters. Default values: lambda =

NULL. If lambda is not provided, the package will give a default lambda sequence; lambda.min.ratio = 1e-04, smallest value for lambda as a fraction of lambda.max (given by default when lambda is NULL); nlambda = 50, number of lambda values (equal spacing on log scale) used when lambda is NULL; alpha = seq(0, 1, length.out = 10), sequence of alpha. Here, alpha is tuning parameter for generalized lasso penalty and 1-alpha is the tuning parameter for

group lasso penalty.

Value

A list of cross validation results.

lambda.min λ value with best prediction performance.

alpha.min α value with best prediction performance.

cvm A (number-of-lambda * number-of-alpha) matrix saving the means of cross val-

idation loss across folds.

cvsd A (number-of-lambda * number-of-alpha) matrix saving standard deviations of

cross validation loss across folds.

TSLA.fit Outputs from TSLA.fit().

Intercept.min Intercept corresponding to (lambda.min,alpha.min).

cov.min Coefficients of unpenalized features corresponding to (lambda.min,alpha.min).

beta.min Coefficients of binary features corresponding to (lambda.min,alpha.min).

gamma.min Node coefficients corresponding to (lambda.min,alpha.min).

groupnorm.min Group norms of node coefficients corresponding to (lambda.min,alpha.min).

lambda.min.index

Index of the best λ in the sequence.

alpha.min.index

Index of the best α in the sequence.

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Examples

```
# Load the synthetic data
data(ClassificationExample)
tree.org <- ClassificationExample$tree.org # original tree structure</pre>
x2.org <- ClassificationExample$x.org</pre>
                                             # original design matrix
x1 <- ClassificationExample$x1</pre>
y <- ClassificationExample$y</pre>
                                           # response
# Do the tree-guided expansion
expand.data <- getetmat(tree.org, x2.org)</pre>
x2 <- expand.data$x.expand
                                           # expanded design matrix
tree.expand <- expand.data$tree.expand # expanded tree structure</pre>
# Do train-test split
idtrain <- 1:200
x1.train <- as.matrix(x1[idtrain, ])</pre>
x2.train <- x2[idtrain, ]</pre>
y.train <- y[idtrain, ]</pre>
x1.test <- as.matrix(x1[-idtrain, ])</pre>
x2.test <- x2[-idtrain, ]</pre>
y.test <- y[-idtrain, ]</pre>
# specify some model parameters
set.seed(100)
control <- list(maxit = 100, mu = 1e-3, tol = 1e-5, verbose = FALSE)</pre>
modstr <- list(nlambda = 5, alpha = seq(0, 1, length.out = 5))
simu.cv <- cv.TSLA(y = y.train, as.matrix(x1[idtrain, ]),</pre>
                    X_2 = x2.train,
                    treemat = tree.expand, family = 'logit',
                    penalty = 'CL2', pred.loss = 'AUC',
                    gamma.init = NULL, weight = c(1, 1), nfolds = 5,
                    group.weight = NULL, feature.weight = NULL,
                    control = control, modstr = modstr)
# Do prediction with the selected tuning parameters on the test set. Report AUC on the test set.
rmid <- simu.cv$TSLA.fit$rmid # remove all zero columns</pre>
if(length(rmid) > 0){
  x2.test <- x2.test[, -rmid]}</pre>
  y.new <- predict_cvTSLA(simu.cv, as.matrix(x1[-idtrain, ]), x2.test)</pre>
  library(pROC)
  auc(as.vector(y.test), as.vector(y.new))
```

getaggr

Generate aggregated features

Description

Function that generates aggregated features based on the TSLA output.

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Usage

```
getaggr(TSLA.object, X_2, X_2.org, lambda.index, alpha.index)
```

Arguments

TSLA.object A fit output from TSLA.fit(), or the TSLA.fit object in cv.TSLA().

X_2 Expanded design matrix in matrix form.X_2.org Original design matrix in matrix form.

lambda.index Index of the λ value selected.

alpha.index Index of the α value selected. The α is the tuning parameter for generalized

lasso penalty.

Value

A data frame of the aggregated feature.

dataset aggregated features.

getetmat Tree-guided expansion

Description

Give the expanded design matrix and the expanded tree structure by adding interactions in conformity to the structure.

Usage

```
getetmat(tmatrix, dmatrix)
```

Arguments

tmatrix Tree structure of the original features in matrix form.

dmatrix Original design matrix in matrix form.

Details

This function is used by the TSLA method only when the penalty is selected as "CL2". The all zero columns produced by the interactions are excluded in the output.

For the TSLA method, the signs of the coefficients in the linear constraints depend on the order of the term. To better extend the method in implementation, we apply the signs on the feature vectors instead of the regression coefficients. For example, we use feature vector $-x_{12}$ instead of x_{12} . The expanded design matrix x.expand from this function is adjusted by the signs. The A matrix and all the coefficients estimated from the package can be explained correspondingly. We also provide x.expand.adj, A.adj, and beta.coef.adj as the quantities with the effects of the signs removed.

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The input tree structure of the original features needs to be constructed as the following: each row corresponds to a variable at the finest level; each column corresponds to an ordered classification level with the leaf level at the left-most and the root level at the right-most; the entry values in each column are the index of the ancestor node of the variable at that level. As we move from left to right, the number of unique values in the column becomes fewer.

Value

A list.

x.expand The design matrix after expansion. Each column is multiplied by $(-1)^{r-1}$,

where r is the order of the corresponding interaction term.

tree.expand The tree structure after expansion.

x.expand.adj The design matrix after expansion with the effects of signs removed.

getperform

Get performance metrics for classification

Description

Evaluate the prediction performance under the classification settings.

Usage

```
getperform(
  ytest,
  ypretest,
  family,
  threshold.method = c("youden", "specificity.control", "quantile"),
  specificity = NULL
)
```

Arguments

ytest Response vector for test data.

ypretest Predicted probability for test data.

family "Is" or "logic". Return MSE when "Is" is used.

threshold.method

Method to get the threshold.

specificity User-defined specificity or quantile.

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Details

The function supports three methods to select the threshold of the predicted probability.

threshold.method = "youden": The optimal threshold corresponds to the point that maximizes the distance to the identity (diagonal) line on the ROC curve.

threshold.method = "specificity.control": The optimal threshold corresponds to the smallest value that ensures the required specificity value.

threshold.method = "quantile": The optimal threshold corresponds to the required quantile of the predicted probability.

Value

List of measures.

AUC Area under the ROC curve.

AUPRC Area under the precision-recall curve.

threshold Selected threshold of the probability.

sensitivity Sensitivity with the selected threshold.

ppv Positive predictive value with the selected threshold.

specificity Specificity with the selected threshold.

true.positive Number of true positive with the selected threshold. false.positive Number of false positive with the selected threshold.

get_tree_object Tree-guided reparameterization

Description

This function generates all the intermediate quantities based on the tree-guided reparameterization.

Usage

```
get_tree_object(
   X_2,
   treemat,
   penalty = c("CL2", "DL2", "RFS-Sum"),
   group.weight = NULL,
   feature.weight = NULL
)
```

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Arguments

X_2 Expanded design matrix for penalty = "CL2"; Original design matrix for penalty = "RFS-Sum". Need to be in the matrix form.

treemat Expanded tree structure for penalty = "CL2"; Original structure for penalty = "RFS-Sum". Need to be in the matrix form.

penalty Two options for group penalty on γ , "CL2" or "RFS-Sum".

group.weight User-defined weights for group penalty. Need to be a vector and the length equals to the number of groups.

feature.weight User-defined weights for each predictor after expansion.

Value

A list consists of quantities needed for SPG optimization.

C_1	C_1 matrix for generalized lasso penalty.
CNorm_1	Nuclear norm of matrix C_1.
C_2	C_2 matrix for group lasso penalty.
CNorm_2	Nuclear norm of matrix C_2.
A	A (number-of-leaf * number-of-node) binary matrix containing linear constraints. Recall that $\beta=A\gamma$. It is used with beta.coef and x.expand.
g_idx	A (number-of-group * 3) matrix. Each column stands for starting row in C_2 of a group, end row in C_2 of a group, and the group size.
M2	A (number-of-leaf * number-of-level) node index matrix, with index going from 1 to the number of nodes. Root node has index equal to the number of nodes. Each row corresponds to a variable at the finest level, each column corresponds to an ordered classification level; the entry values in each column are the unique indices of the variables at that level. As we move to the right, the number of unique values becomes fewer.
Tree	A (number-of-group * number-of-node) group index matrix. Each row is a group and the column order is the same as the order of node index in M2. If the jth node belongs to the ith group, then the (i, j) element of the matrix is 1; otherwise the element is 0.
A.adj	A (number-of-leaf * number-of-node) binary matrix containing linear constraints. It is used with beta.coef.adj and x.expand.adj.

plot_TSLA	Plot aggregated structure	
btot_12FV	Pioi aggregatea structure	

Description

Return a tree plot.

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Usage

```
plot_TSLA(TSLA.object, X_2, X_2.org, lambda.index, alpha.index)
```

Arguments

TSLA.object A fit output from TSLA.fit(), or the TSLA.fit object in cv.TSLA(). X_2 Expanded design matrix in matrix form.

X_2.org Original design matrix in matrix form.

lambda.index Index of the λ value selected.

alpha.index Index of the α value selected. The α is the tuning parameter for generalized

lasso penalty.

Value

A plot

Examples

```
# Load the synthetic data
data(ClassificationExample)
tree.org <- ClassificationExample$tree.org # original tree structure</pre>
x2.org <- ClassificationExample$x.org</pre>
                                              # original design matrix
x1 <- ClassificationExample$x1</pre>
y <- ClassificationExample$y</pre>
                                          # response
# Do the tree-guided expansion
expand.data <- getetmat(tree.org, x2.org)</pre>
x2 <- expand.data$x.expand
                                           # expanded design matrix
tree.expand <- expand.data$tree.expand # expanded tree structure</pre>
# Do train-test split
idtrain <- 1:200
x1.train <- as.matrix(x1[idtrain, ])</pre>
x2.train <- x2[idtrain, ]</pre>
y.train <- y[idtrain, ]</pre>
x1.test <- as.matrix(x1[-idtrain, ])</pre>
x2.test <- x2[-idtrain, ]</pre>
y.test <- y[-idtrain, ]</pre>
# specify some model parameters
set.seed(100)
control <- list(maxit = 100, mu = 1e-3, tol = 1e-5, verbose = FALSE)</pre>
modstr \leftarrow list(nlambda = 5, alpha = seq(0, 1, length.out = 5))
simu.cv <- cv.TSLA(y = y.train, as.matrix(x1[idtrain, ]),</pre>
                    X_2 = x2.train,
                    treemat = tree.expand, family = 'logit',
                    penalty = 'CL2', pred.loss = 'AUC',
                    gamma.init = NULL, weight = c(1, 1), nfolds = 5,
                    group.weight = NULL, feature.weight = NULL,
```

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```
control = control, modstr = modstr)
plot_TSLA(simu.cv$TSLA.fit, x2, x2.org, simu.cv$lambda.min.index, simu.cv$alpha.min.index)
```

predict_cvTSLA

Prediction from cross validation

Description

A convenient function to get prediction from the selected tuning parameters by cross validation.

Usage

```
predict_cvTSLA(
  object,
  X_1_new = NULL,
  X_2_new,
  type = c("response", "link"),
  ...
)
```

Other parameters.

Arguments

object A fit output from cv.TSLA().

X_1_new New unpenalized features in matrix form.

X_2_new New binary features in matrix form.

type Two options: "response" or "link". The two options only differ for family="logit".

Value

. . .

Predictions.

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Prediction from TSLA with new data

Description

Generate prediction for the response.

Usage

```
predict_TSLA(
  object,
  X_1_new = NULL,
  X_2_new,
  type = c("response", "link"),
  ...
)
```

Arguments

object	A fit output from TSLA.fit().
X_1_new	New unpenalized features in matrix form.
X_2_new	New binary features in matrix form.
type	Two options: "response" or "link". The two options only differ for family="logit".
	Other parameters.

Value

Predictions. The first dimension is indexed by the observation, the second dimension is indexed by λ , and the third dimension is indexed by α .

 ${\tt RegressionExample}$

Synthesic for the regression example

Description

Synthetic data used to illustrate how to use TSLA with regression.

Usage

```
data(RegressionExample)
```

TSLA.fit

Format

List containing the following elements:

tree.org Original tree structure with 42 leaf nodes and 5 different levels.

x.org Original design matrix with 42 binary features and 400 observations.

y Continuous response of length 400.

TSLA.fit

Solve the TSLA optimization problem

Description

Find the solutions with a Smoothing Proximal Gradient (SPG) algorithm for a sequence of α and λ values.

Usage

```
TSLA.fit(
   y,
   X_1 = NULL,
   X_2,
   treemat,
   family = c("ls", "logit"),
   penalty = c("CL2", "RFS-Sum"),
   gamma.init = NULL,
   weight = NULL,
   group.weight = NULL,
   feature.weight = NULL,
   control = list(),
   modstr = list()
)
```

Arguments

У	Response in matrix form, continuous for family = "ls" and binary (0/1) for family = "logit".
X_1	Design matrix for unpenalized features (excluding intercept). Need to be in the matrix form.
X_2	Expanded design matrix for penalty = "CL2"; Original design matrix for penalty = "RFS-Sum". Need to be in the matrix form.
treemat	Expanded tree structure in matrix form for penalty = "CL2"; Original structure for penalty = "RFS-Sum".
family	Two options. Use "ls" for least square problems and "logit" for logistic regression problems.
penalty	Two options for group penalty on γ , "CL2" or "RFS-Sum".

TSLA.fit

gamma.init Initial value for the optimization. Default is a zero vector. The length should

equal to 1+ncol(X_1)+ncol(A). See details of A in get_tree_obj().

weight A vector of length two and it is used for logistic regression only. The first

element corresponds to weight of y=1 and the second element corresponds to

weight of y=0.

group.weight User-defined weights for group penalty. Need to be a vector and the length

equals to the number of groups.

feature.weight User-defined weights for each predictor after expansion.

control A list of parameters controlling algorithm convergence. Default values: tol =

1e-5, convergence tolerance; maxit = 10000, maximum number of iterations;

mu = 1e-3, smoothness parameter in SPG.

modstr A list of parameters controlling tuning parameters. Default values: lambda =

NULL. If lambda is not provided, the package will give a default lambda sequence; lambda.min.ratio = 1e-04, smallest value for lambda as a fraction of lambda.max (given by default when lambda is NULL); nlambda = 50, number of lambda values (equal spacing on log scale) used when lambda is NULL; alpha = seq(0, 1, length.out = 10), sequence of alpha. Here, alpha is tuning parameter for generalized lasso penalty and 1-alpha is the tuning parameter for

group lasso penalty.

Details

We adopt the warm start technique to speed up the calculation. The warm start is applied with a fixed value of α and a descending sequence of λ .

The objective function for "ls" is

$$1/2RSS + \lambda(\alpha P(\beta) + (1 - \alpha)P(\gamma)),$$

subject to $\beta = A\gamma$. The objective function for "logit" is

$$-log lik + \lambda(\alpha P(\beta) + (1 - \alpha)P(\gamma)),$$

subject to $\beta = A\gamma$. Note that, in this package, the input parameter "alpha" is the tuning parameter for the generalized lasso penalty.

Details for "penalty" option:

For penalty = "CL2", see details for the "Child-12" penalty in the main paper.

For penalty = "RFS-Sum", the theoretical optimal weights are used. Please check the details in paper "Rare feature selection in high dimensions".

Value

A list of model fitting results.

gammacoef Estimation for γ .

groupnorm Weighted norms for each group.

lambda.seq Sequence of λ values.

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alpha.seq Tuning parameter sequence for the generalized lasso penalty.

rmid Column index for all zero features.

family Option of family.

cov.name Names for unpenalized features.

bin.name Names for binary feautres.

tree.object Outputs from get_tree_obj().

References

Chen, J., Aseltine, R. H., Wang, F., & Chen, K. (2024). *Tree-Guided Rare Feature Selection and Logic Aggregation with Electronic Health Records Data. Journal of the American Statistical Association* 119(547), 1765-1777, doi:10.1080/01621459.2024.2326621.

Chen, X., Q. Lin, S. Kim, J. G. Carbonell, and E. P. Xing (2012). *Smoothing proximal gradient method for general structured sparse regression. The Annals of Applied Statistics* 6(2), 719–752, doi:10.1214/11AOAS514.

Yan, X. and J. Bien (2021). Rare feature selection in high dimensions. Journal of the American Statistical Association 116(534), 887–900, doi:10.1080/01621459.2020.1796677.

Examples

```
# Load the synthetic data
data(RegressionExample)
tree.org <- RegressionExample$tree.org # original tree structure</pre>
x2.org <- RegressionExample$x.org</pre>
                                        # original design matrix
y <- RegressionExample$y</pre>
                                     # response
# Do the tree-guided expansion
expand.data <- getetmat(tree.org, x2.org)</pre>
x2 <- expand.data$x.expand
                                         # expanded design matrix
tree.expand <- expand.data$tree.expand # expanded tree structure
# specify some model parameters
set.seed(100)
control <- list(maxit = 100, mu = 1e-3, tol = 1e-5, verbose = FALSE)</pre>
# fit model with a pair of lambda and alpha
modstr <- list(lambda = 1, alpha = 0.1)</pre>
x1 <- NULL
fit1 <- TSLA.fit(y, x1, x2, tree.expand, family = 'ls',
                 penalty = 'CL2',
                 gamma.init = NULL, weight = NULL,
                 group.weight = NULL, feature.weight = NULL,
                 control, modstr)
# get group norms from fit1
fit1$groupnorm
```

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