

Package ‘orf’

October 14, 2022

Type Package

Title Ordered Random Forests

Version 0.1.4

Date 2022-07-21

Author Gabriel Okasa [aut, cre], Michael Lechner [ctb]

Maintainer Gabriel Okasa <okasa.gabriel@gmail.com>

Description An implementation of the Ordered Forest estimator as developed in Lechner & Okasa (2019) <[arXiv:1907.02436](#)>. The Ordered Forest flexibly estimates the conditional probabilities of models with ordered categorical outcomes (so-called ordered choice models). Additionally to common machine learning algorithms the 'orf' package provides functions for estimating marginal effects as well as statistical inference thereof and thus provides similar output as in standard econometric models for ordered choice. The core forest algorithm relies on the fast C++ forest implementation from the 'ranger' package (Wright & Ziegler, 2017) <[arXiv:1508.04409](#)>.

License GPL-3

Encoding UTF-8

LazyData true

Depends R (>= 2.10)

Imports ggplot2, ranger, Rcpp, stats, utils, xtable

RoxygenNote 7.2.1

Suggests knitr, rmarkdown, testthat

VignetteBuilder knitr

URL <https://github.com/okasag/orf>

BugReports <https://github.com/okasag/orf/issues>

LinkingTo Rcpp

NeedsCompilation yes

Repository CRAN

Date/Publication 2022-07-23 22:40:02 UTC

R topics documented:

orf-package	2
margins	3
margins.orf	4
odata	6
orf	8
plot.orf	11
predict.orf	12
print.margins.orf	13
print.orf	14
print.orf.prediction	15
summary.margins.orf	16
summary.orf	18
summary.orf.prediction	19

Index	21
--------------	-----------

orf-package	<i>orf: Ordered Random Forests</i>
-------------	------------------------------------

Description

An implementation of the Ordered Forest estimator as developed in Lechner & Okasa (2019). The Ordered Forest flexibly estimates the conditional probabilities of models with ordered categorical outcomes (so-called ordered choice models). Additionally to common machine learning algorithms the orf package provides functions for estimating marginal effects as well as statistical inference thereof and thus provides similar output as in standard econometric models for ordered choice. The core forest algorithm relies on the fast C++ forest implementation from the ranger package (Wright & Ziegler, 2017).

Author(s)

Gabriel Okasa, Michael Lechner

References

- Lechner, M., & Okasa, G. (2019). Random Forest Estimation of the Ordered Choice Model. arXiv preprint arXiv:1907.02436. <https://arxiv.org/abs/1907.02436>
- Goller, D., Knaus, M. C., Lechner, M., & Okasa, G. (2021). Predicting Match Outcomes in Football by an Ordered Forest Estimator. *A Modern Guide to Sports Economics*. Edward Elgar Publishing, 335-355. doi:10.4337/9781789906530.00026
- Wright, M. N. & Ziegler, A. (2017). ranger: A fast implementation of random forests for high dimensional data in C++ and R. *J Stat Softw* 77:1-17. doi:10.18637/jss.v077.i01.

Examples

```
## Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates
Y <- as.numeric(odata[, 1])
X <- as.matrix(odata[, -1])

# estimate Ordered Forest with default settings
orf_fit <- orf(X, Y)

# print output of the orf estimation
print(orf_fit)

# show summary of the orf estimation
summary(orf_fit)

# plot the estimated probability distributions
plot(orf_fit)

# predict with the estimated orf
predict(orf_fit)

# estimate marginal effects of the orf
margins(orf_fit)
```

margins

Marginal Effects

Description

S3 generic method for estimation of marginal effects of an Ordered Forest objects of class orf.

Usage

```
margins(forest, eval = NULL, inference = NULL, window = NULL, newdata = NULL)
```

Arguments

forest	estimated Ordered Forest object of class orf
eval	string, defining evaluation point for marginal effects. These can be one of "mean", "atmean", or "atmedian". (Default is "mean")
inference	logical, if TRUE inference on marginal effects will be conducted (default is inherited from the orf object)

window	numeric, share of standard deviation of X to be used for evaluation of the marginal effect (default is 0.1)
newdata	numeric matrix X containing the new observations for which the marginal effects should be estimated

Author(s)

Gabriel Okasa

See Also

[margins.orf](#), [summary.margins.orf](#) and [print.margins.orf](#)

Examples

```
## Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates
Y <- as.numeric(odata[, 1])
X <- as.matrix(odata[, -1])

# estimate Ordered Forest
orf_fit <- orf(X, Y)

# estimate default marginal effects of the orf
orf_margins <- margins(orf_fit)
```

margins.orf

Marginal Effects for the Ordered Forest

Description

S3 method for estimation of marginal effects of an Ordered Forest objects of class orf.

Usage

```
## S3 method for class 'orf'
margins(forest, eval = NULL, inference = NULL, window = NULL, newdata = NULL)
```

Arguments

forest	estimated Ordered Forest object of class orf
eval	string, defining evaluation point for marginal effects. These can be one of "mean", "atmean", or "atmedian". (Default is "mean")
inference	logical, if TRUE inference on marginal effects will be conducted (default is inherited from the orf object)
window	numeric, share of standard deviation of X to be used for evaluation of the marginal effect (default is 0.1)
newdata	numeric matrix X containing the new observations for which the marginal effects should be estimated

Details

margins.orf estimates marginal effects at the mean, at the median, or the mean marginal effects, depending on the eval argument. It is advised to increase the number of subsampling replications in the supplied orf object as the estimation of the marginal effects is a more demanding exercise than a simple Ordered Forest estimation/prediction. Additionally to the estimation of the marginal effects, the weight-based inference for the effects is supported as well. Note, that the inference procedure is much more computationally exhausting exercise due to the computation of the forest weights. Additionally, the evaluation window for the marginal effects can be regulated through the window argument. Furthermore, new data for which marginal effects should be computed can be supplied as well as long as it lies within the support of X.

Value

object of type margins.orf with following elements

info	info containing forest inputs and data used
effects	marginal effects
variances	variances of marginal effects
errors	standard errors of marginal effects
tvalues	t-values of marginal effects
pvalues	p-values of marginal effects

Author(s)

Gabriel Okasa

See Also

[summary.margins.orf](#), [print.margins.orf](#)

Examples

```
## Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates
Y <- as.numeric(odata[, 1])
X <- as.matrix(odata[, -1])

# estimate Ordered Forest
orf_fit <- orf(X, Y)

# estimate marginal effects of the orf (default)
orf_margins <- margins(orf_fit)

# estimate marginal effects evaluated at the mean
orf_margins <- margins(orf_fit, eval = "atmean")

# estimate marginal effects with inference
# (orf object has to be estimated with honesty and subsampling)
orf_margins <- margins(orf_fit, inference = TRUE)

# estimate marginal effects with custom window size
orf_margins <- margins(orf_fit, window = 0.5)

# estimate marginal effects for some new data (within support of X)
orf_margins <- margins(orf_fit, newdata = X[1:10, ])

# estimate marginal effects with all custom settings
orf_margins <- margins(orf_fit, eval = "atmedian", inference = TRUE,
                      window = 0.5, newdata = X[1:10, ])
```

odata

Simulated Example Dataset

Description

A simulated example dataset with ordered categorical outcome variable containing different types of covariates for illustration purposes.

Usage

odata

Format

A data frame with 1000 rows and 5 variables

Details

For the exact data generating process, see the example below.

Value

Y	ordered outcome, classes 1, 2, and 3
X1	continuous covariate, $N(0,1)$
X2	categorical covariate, values 1, 2, and 3
X3	binary covariate, values 0 and 1
X4	continuous covariate, $N(0,10)$

Examples

```
# generate example data

# set seed for replicability
set.seed(123)

# number of observations
n <- 1000

# various covariates
X1 <- rnorm(n, 0, 1) # continuous
X2 <- rbinom(n, 2, 0.5) # categorical
X3 <- rbinom(n, 1, 0.5) # dummy
X4 <- rnorm(n, 0, 10) # noise

# bind into matrix
X <- as.matrix(cbind(X1, X2, X3, X4))

# deterministic component
deterministic <- X1 + X2 + X3
# generate continuous outcome with logistic error
Y <- deterministic + rlogis(n, 0, 1)
# thresholds for continuous outcome
cuts <- quantile(Y, c(0, 1/3, 2/3, 1))
# discretize outcome into ordered classes 1, 2, 3
Y <- as.numeric(cut(Y, breaks = cuts, include.lowest = TRUE))

# save data as a dataframe
odata <- as.data.frame(cbind(Y, X))

# end of data generating
```

 orf

Ordered Forest Estimator

Description

An implementation of the Ordered Forest estimator as developed in Lechner & Okasa (2019). The Ordered Forest flexibly estimates the conditional probabilities of models with ordered categorical outcomes (so-called ordered choice models). Additionally to common machine learning algorithms the orf package provides functions for estimating marginal effects as well as statistical inference thereof and thus provides similar output as in standard econometric models for ordered choice. The core forest algorithm relies on the fast C++ forest implementation from the ranger package (Wright & Ziegler, 2017).

Usage

```
orf(
  X,
  Y,
  num.trees = 1000,
  mtry = NULL,
  min.node.size = NULL,
  replace = FALSE,
  sample.fraction = NULL,
  honesty = TRUE,
  honesty.fraction = NULL,
  inference = FALSE,
  importance = FALSE
)
```

Arguments

X	numeric matrix of features
Y	numeric vector of outcomes
num.trees	scalar, number of trees in a forest, i.e. bootstrap replications (default is 1000 trees)
mtry	scalar, number of randomly selected features (default is the squared root of number of features, rounded up to the nearest integer)
min.node.size	scalar, minimum node size, i.e. leaf size of a tree (default is 5 observations)
replace	logical, if TRUE sampling with replacement, i.e. bootstrap is used to grow the trees, otherwise subsampling without replacement is used (default is set to FALSE)
sample.fraction	scalar, subsampling rate (default is 1 for bootstrap and 0.5 for subsampling)
honesty	logical, if TRUE honest forest is built using sample splitting (default is set to TRUE)

honesty.fraction	scalar, share of observations belonging to honest sample not used for growing the forest (default is 0.5)
inference	logical, if TRUE the weight based inference is conducted (default is set to FALSE)
importance	logical, if TRUE variable importance measure based on permutation is conducted (default is set to FALSE)

Details

The Ordered Forest function, `orf`, estimates the conditional ordered choice probabilities, i.e. $P[Y=m|X=x]$. Additionally, weight-based inference for the probability predictions can be conducted as well. If inference is desired, the Ordered Forest must be estimated with honesty and subsampling. If prediction only is desired, estimation without honesty and with bootstrapping is recommended for optimal prediction performance.

In order to estimate the Ordered Forest user must supply the data in form of matrix of covariates X and a vector of outcomes `codeY` to the `orf` function. These data inputs are also the only inputs that must be specified by the user without any defaults. Further optional arguments include the classical forest hyperparameters such as number of trees, `num.trees`, number of randomly selected features, `mtry`, and the minimum leaf size, `min.node.size`. The forest building scheme is regulated by the `replace` argument, meaning bootstrapping if `replace = TRUE` or subsampling if `replace = FALSE`. For the case of subsampling, `sample.fraction` argument regulates the subsampling rate. Further, honest forest is estimated if the `honesty` argument is set to `TRUE`, which is also the default. Similarly, the fraction of the sample used for the honest estimation is regulated by the `honesty.fraction` argument. The default setting conducts a 50:50 sample split, which is also generally advised to follow for optimal performance. Inference procedure of the Ordered Forest is based on the forest weights and is controlled by the `inference` argument. Note, that such weight-based inference is computationally demanding exercise due to the estimation of the forest weights and as such longer computation time is to be expected. Lastly, the `importance` argument turns on and off the permutation based variable importance.

`orf` is compatible with standard R commands such as `predict`, `margins`, `plot`, `summary` and `print`. For further details, see examples below.

Value

object of type `orf` with following elements

<code>forests</code>	saved forests trained for <code>orf</code> estimations (inherited from <code>ranger</code>)
<code>info</code>	info containing forest inputs and data used
<code>predictions</code>	predicted values for class probabilities
<code>variances</code>	variances of predicted values
<code>importance</code>	weighted measure of permutation based variable importance
<code>accuracy</code>	oob measures for mean squared error and ranked probability score

Author(s)

Gabriel Okasa

References

- Lechner, M., & Okasa, G. (2019). Random Forest Estimation of the Ordered Choice Model. arXiv preprint arXiv:1907.02436. <https://arxiv.org/abs/1907.02436>
- Goller, D., Knaus, M. C., Lechner, M., & Okasa, G. (2021). Predicting Match Outcomes in Football by an Ordered Forest Estimator. A Modern Guide to Sports Economics. Edward Elgar Publishing, 335-355. doi:10.4337/9781789906530.00026
- Wright, M. N. & Ziegler, A. (2017). ranger: A fast implementation of random forests for high dimensional data in C++ and R. J Stat Softw 77:1-17. doi:10.18637/jss.v077.i01.

See Also

[summary.orf](#), [plot.orf](#) [predict.orf](#), [margins.orf](#)

Examples

```
## Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates
Y <- as.numeric(odata[, 1])
X <- as.matrix(odata[, -1])

# estimate Ordered Forest with default parameters
orf_fit <- orf(X, Y)

# estimate Ordered Forest with own tuning parameters
orf_fit <- orf(X, Y, num.trees = 2000, mtry = 3, min.node.size = 10)

# estimate Ordered Forest with bootstrapping and without honesty
orf_fit <- orf(X, Y, replace = TRUE, honesty = FALSE)

# estimate Ordered Forest with subsampling and with honesty
orf_fit <- orf(X, Y, replace = FALSE, honesty = TRUE)

# estimate Ordered Forest with subsampling and with honesty
# with own tuning for subsample fraction and honesty fraction
orf_fit <- orf(X, Y, replace = FALSE, sample.fraction = 0.5,
              honesty = TRUE, honesty.fraction = 0.5)

# estimate Ordered Forest with subsampling and with honesty and with inference
# (for inference, subsampling and honesty are required)
orf_fit <- orf(X, Y, replace = FALSE, honesty = TRUE, inference = TRUE)

# estimate Ordered Forest with simple variable importance measure
orf_fit <- orf(X, Y, importance = TRUE)

# estimate Ordered Forest with all custom settings
orf_fit <- orf(X, Y, num.trees = 2000, mtry = 3, min.node.size = 10,
```

```
replace = TRUE, sample.fraction = 1,  
honesty = FALSE, honesty.fraction = 0,  
inference = FALSE, importance = FALSE)
```

plot.orf

Plot of the Ordered Forest

Description

plot the probability distributions estimated by the Ordered Forest object of class orf

Usage

```
## S3 method for class 'orf'  
plot(x, ...)
```

Arguments

x	estimated Ordered Forest object of class orf
...	further arguments (currently ignored)

Details

plot.orf generates probability distributions, i.e. density plots of estimated ordered probabilities by the Ordered Forest for each outcome class considered. The plots effectively visualize the estimated probability density in contrast to a real observed ordered outcome class and as such provide a visual inspection of the overall in-sample estimation accuracy. The dashed lines locate the means of the respective probability distributions.

Author(s)

Gabriel Okasa

Examples

```
# Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates  
Y <- as.numeric(odata[, 1])  
X <- as.matrix(odata[, -1])  
  
# estimate Ordered Forest  
orf_fit <- orf(X, Y)
```

```
# plot the estimated probability distributions
plot(orf_fit)
```

predict.orf *Prediction of the Ordered Forest*

Description

Prediction for new observations based on estimated Ordered Forest of class orf

Usage

```
## S3 method for class 'orf'
predict(object, newdata = NULL, type = NULL, inference = NULL, ...)
```

Arguments

object	estimated Ordered Forest object of class orf
newdata	numeric matrix X containing the observations for which the outcomes should be predicted
type	string, specifying the type of the prediction, These can be either "probs" or "p" for probabilities and "class" or "c" for classes. (Default is "probs").
inference	logical, if TRUE variances for the predictions will be estimated (only feasible for probability predictions).
...	further arguments (currently ignored)

Details

predict.orf estimates the conditional ordered choice probabilities, i.e. $P[Y=m|X=x]$ for new data points (matrix X containing new observations of covariates) based on the estimated Ordered Forest object of class orf. Furthermore, weight-based inference for the probability predictions can be conducted as well. If inference is desired, the supplied Ordered Forest must be estimated with honesty and subsampling. If prediction only is desired, estimation without honesty and with bootstrapping is recommended for optimal prediction performance. Additionally to the probability predictions, class predictions can be estimated as well using the type argument. In this case, the predicted classes are obtained as classes with the highest predicted probability.

Value

object of class orf.prediction with following elements

info	info containing forest inputs and data used
predictions	predicted values
variances	variances of predicted values

Author(s)

Gabriel Okasa

See Also[summary.orf.prediction](#), [print.orf.prediction](#)**Examples**

```
# Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates for train and test
idx <- sample(seq(1, nrow(odata), 1), 0.8*nrow(odata))

# train set
Y_train <- as.numeric(odata[idx, 1])
X_train <- as.matrix(odata[idx, -1])

# test set
Y_test <- as.numeric(odata[-idx, 1])
X_test <- as.matrix(odata[-idx, -1])

# estimate Ordered Forest
orf_fit <- orf(X_train, Y_train)

# predict the probabilities with the estimated orf
orf_pred <- predict(orf_fit, newdata = X_test)

# predict the probabilities with estimated orf together with variances
orf_pred <- predict(orf_fit, newdata = X_test, inference = TRUE)

# predict the classes with estimated orf
orf_pred <- predict(orf_fit, newdata = X_test, type = "class")
```

`print.margins.orf`*Print of the Ordered Forest Marginal Effects*

Description

print of estimated marginal effects of the Ordered Forest of class margins.orf

Usage

```
## S3 method for class 'margins.orf'  
print(x, ...)
```

Arguments

x estimated Ordered Forest Marginal Effect object of type margins.orf
... further arguments (currently ignored)

Details

print.margins.orf provides a first glimpse of the Ordered Forest marginal effects, printed directly to the R console. The printed information contains the results for the marginal effects for each covariate and each outcome class.

Author(s)

Gabriel Okasa

Examples

```
## Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates  
Y <- as.numeric(odata[, 1])  
X <- as.matrix(odata[, -1])  
  
# estimate Ordered Forest  
orf_fit <- orf(X, Y)  
  
# estimate marginal effects of the orf  
orf_margins <- margins(orf_fit)  
  
# print marginal effects  
print(orf_margins)
```

print.orf

Print of the Ordered Forest

Description

print of an estimated Ordered Forest object of class orf

Usage

```
## S3 method for class 'orf'  
print(x, ...)
```

Arguments

```
x          estimated Ordered Forest object of class orf  
...        further arguments (currently ignored)
```

Details

print.orf provides a first glimpse of the Ordered Forest estimation, printed directly to the R console. The printed information contains the main inputs of the orf function.

Author(s)

Gabriel Okasa

Examples

```
# Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates  
Y <- as.numeric(odata[, 1])  
X <- as.matrix(odata[, -1])  
  
# estimate Ordered Forest  
orf_fit <- orf(X, Y)  
  
# print output of the orf estimation  
print(orf_fit)
```

print.orf.prediction *Print of the Ordered Forest Prediction*

Description

print of Ordered Forest predictions of class orf.prediction

Usage

```
## S3 method for class 'orf.prediction'  
print(x, ...)
```

Arguments

x predicted Ordered Forest object of class orf.prediction
... further arguments (currently ignored)

Details

print.orf.prediction provides a first glimpse of the Ordered Forest prediction, printed directly to the R console. The printed information contains the main inputs of the predict.orf function.

Author(s)

Gabriel Okasa

Examples

```
# Ordered Forest
require(orf)

# load example data
data(odata)

# specify response and covariates for train and test
idx <- sample(seq(1, nrow(odata), 1), 0.8*nrow(odata))

# train set
Y_train <- as.numeric(odata[idx, 1])
X_train <- as.matrix(odata[idx, -1])

# test set
Y_test <- as.numeric(odata[-idx, 1])
X_test <- as.matrix(odata[-idx, -1])

# estimate Ordered Forest
orf_fit <- orf(X_train, Y_train)

# predict the probabilities with the estimated orf
orf_pred <- predict(orf_fit, newdata = X_test)

# print the prediction object
print(orf_pred)
```

summary.margins.orf *Summary of the Ordered Forest Marginal Effects*

Description

summary of estimated marginal effects of the Ordered Forest of class margins.orf

Usage

```
## S3 method for class 'margins.orf'  
summary(object, latex = FALSE, ...)
```

Arguments

object	estimated Ordered Forest Marginal Effect object of type margins.orf
latex	logical, if TRUE latex coded summary will be generated (default is FALSE)
...	further arguments (currently ignored)

Details

summary.margins.orf provides estimation results of the Ordered Forest marginal effects. The summary contains the results for the marginal effects for each covariate and each outcome class, optionally with inference as well. Furthermore, summary output as a LaTeX table is supported in order to directly extract the results for the documentation.

Author(s)

Gabriel Okasa

Examples

```
## Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates  
Y <- as.numeric(odata[, 1])  
X <- as.matrix(odata[, -1])  
  
# estimate Ordered Forest  
orf_fit <- orf(X, Y)  
  
# estimate marginal effects of the orf  
orf_margins <- margins(orf_fit)  
  
# summary of marginal effects  
summary(orf_margins)  
  
# summary of marginal effects coded in LaTeX  
summary(orf_margins, latex = TRUE)
```

`summary.orf`*Summary of the Ordered Forest*

Description

summary of an estimated Ordered Forest object of class orf

Usage

```
## S3 method for class 'orf'  
summary(object, latex = FALSE, ...)
```

Arguments

object	estimated Ordered Forest object of class orf
latex	logical, if TRUE latex coded summary will be generated (default is FALSE)
...	further arguments (currently ignored)

Details

summary.orf provides a short summary of the Ordered Forest estimation, including the input information regarding the values of hyperparameters as well as the output information regarding the prediction accuracy.

Author(s)

Gabriel Okasa

Examples

```
# Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates  
Y <- as.numeric(odata[, 1])  
X <- as.matrix(odata[, -1])  
  
# estimate Ordered Forest  
orf_fit <- orf(X, Y)  
  
# show summary of the orf estimation  
summary(orf_fit)  
  
# show summary of the orf estimation coded in LaTeX  
summary(orf_fit, latex = TRUE)
```

`summary.orf.prediction`*Summary of the Ordered Forest Prediction*

Description

summary of Ordered Forest predictions of class `orf.prediction`

Usage

```
## S3 method for class 'orf.prediction'  
summary(object, latex = FALSE, ...)
```

Arguments

<code>object</code>	predicted Ordered Forest object of class <code>orf.prediction</code>
<code>latex</code>	logical, if TRUE latex coded summary will be generated (default is FALSE)
<code>...</code>	further arguments (currently ignored)

Details

`summary.orf.prediction` provides a main summary of the Ordered Forest prediction, including the input information regarding the values of hyperparameters as well as the inputs of the `predict.orf` function.

Author(s)

Gabriel Okasa

Examples

```
# Ordered Forest  
require(orf)  
  
# load example data  
data(odata)  
  
# specify response and covariates for train and test  
idx <- sample(seq(1, nrow(odata), 1), 0.8*nrow(odata))  
  
# train set  
Y_train <- as.numeric(odata[idx, 1])  
X_train <- as.matrix(odata[idx, -1])  
  
# test set  
Y_test <- as.numeric(odata[-idx, 1])  
X_test <- as.matrix(odata[-idx, -1])
```

```
# estimate Ordered Forest
orf_fit <- orf(X_train, Y_train)

# predict the probabilities with the estimated orf
orf_pred <- predict(orf_fit, newdata = X_test)

# summary of the prediction object
summary(orf_pred)

# show summary of the orf prediction coded in LaTeX
summary(orf_pred, latex = TRUE)
```

Index

* datasets

odata, [6](#)

margins, [3](#)

margins.orf, [4](#), [4](#), [10](#)

odata, [6](#)

orf, [8](#)

orf-package, [2](#)

plot.orf, [10](#), [11](#)

predict.orf, [10](#), [12](#)

print.margins.orf, [4](#), [5](#), [13](#)

print.orf, [14](#)

print.orf.prediction, [13](#), [15](#)

summary.margins.orf, [4](#), [5](#), [16](#)

summary.orf, [10](#), [18](#)

summary.orf.prediction, [13](#), [19](#)